UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS

International General Certificate of Secondary Education

MARK SCHEME for the May/June 2008 question paper

0580, 0581 MATHEMATICS

0580/04, 0581/04 Paper 4 (Extended), maximum raw mark 130

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began.

All Examiners are instructed that alternative correct answers and unexpected approaches in candidates' scripts must be given marks that fairly reflect the relevant knowledge and skills demonstrated.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• CIE will not enter into discussions or correspondence in connection with these mark schemes.

CIE is publishing the mark schemes for the May/June 2008 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.



Page 2	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2008	0580, 0581	04

1 (a) (i)	250	B1		
(ii)	their (a)(i) \div 5 × 52 o.e.	M1	SC1 for $12.5 \div 5 \times 52$, implied by 130	
	2600 ft www2			
(iii)	$\frac{their (a)(ii) - 2450}{2450} \times 100$ o.e.	M1	$\frac{their (a)(ii)}{2450} \times 100 - 100, \ \frac{2450}{100} = \frac{150}{x}$	
	6.1 (22) ft www2	A1ft	ft M & A only if their (a)(ii) > 2450	
(b) (i)	$20 \div 5 \times 3$	M1		
	12 www2	A1	Accept 12, 8 or 8, 12	
(ii)	ii) their (b)(i) \div 3 and (20 – their (b)(i)) \div 2.5		4 and 3.2 or 7.2 or 7h 20 mins seen imply	
			M1	
	7 hours 12 mins cao www2		Condone poor notation e.g. 7-12	
(iii)	2.78 (2.777–2.778) o.e. cao		o.e. must have units stated e.g.	
	o.e. in other units		0.7716m/s, 46.29 – 46.30 m/min	
(iv)	v) 16 07 o.e. ft		ft their (b)(ii) + 08 55 iff finishes on same	
			day and (b)(ii) has hours and mins	
(c)	$20 \times 1000000 \div 80$ o.e.	M1		
	25 000 or 2.5×10^4 www2	A1	25 000 seen in final ans. After M0, SC1	
			for figs 25 or 0.00004 final answer [13]	

2 (a) (i)	(x+4)(x-5)	B2	If B0, SC1 if of form $(x \pm 4)(x \pm 5)$,
(ii)	-4, 5 ft	B1 ft	Only ft the SC
			-4, and 5 not from $(x-4)(x+5)$.
(b)	$(2) + \sqrt{(2)^2 + 43 + 2}$		B1 for $(-2)^2$ -4(3)(-2) (or better) seen
	$\frac{-(-2) \pm \sqrt{(-2)^2 - 4.3 - 2}}{2.3}$	B1,B1	inside a square root.
	2.3		The expression must be in the form
			$\frac{p + (\text{or} -)\sqrt{q}}{r} \text{ then } \mathbf{B1} \text{ for } p = -(-2) \text{ and}$
			1
			r = 2.3 or better
			Allow recoveries from incomplete lines
	-0.55, 1.22 cao	B1,B1	If B0, SC1 for -0.5 and 1.2 or both
			answers correct to 2 or more decimal
			places (rounded or truncated).
			-0.54858, 1.21525
(c) (i)	(m-2n)(m+2n)	B 1	
(ii)	-12	B1	
(iii)			B1 for $(4x^2 + 6x + 6x + 9)$ or
	20x + 5 o.e. cao final ans	B2	$(x^2 - x - x + 1)$ or
			(2x+3-2(x-1))(2x+3+2(x-1))
(iv)	$4n^2 = m^2 - y$ o.e.	M1	$(2x+3-2(x-1))(2x+3+2(x-1))$ M1 for correct re-arrangement for n^2 term
	$m^2 - v$		$(\text{may be } -n^2)$
	$n^2 = \frac{m}{4}$ o.e.	M1	M1 for correct division by 4 or – 4
	4		M1 for correctly taking square root of n^2
	$n^{2} = \frac{m^{2} - y}{4} \text{o.e.}$ $(n) = \sqrt{\frac{m^{2} - y}{4}} \text{o.e.}$ www3	M1	term
	$(n) = \sqrt{\frac{m}{4}}$ o.e. www3		
	Mark final answer		SC2 for $\sqrt{\frac{y \pm m^2}{4}}$ or $\sqrt{\frac{m^2 - y}{4}}$ o.e. ww
			V 4 V 4
(d) (i)	4 or -4 or ±4	B 1	
(ii)	$n(m^4 - 16n^4)$ or	M1	Correctly taking out <i>n</i> or a correct factor
	$(m^2n - 4n^3)(m^2 + 4n^2)$ or		with <i>n</i> still in one bracket
	$(m^2n + 4n^3)(m^2 - 4n^2)$ or		
	$n(m-2n)(m+2n)(m^2+4n^2)$	A1	Must be final answer [17]

Page 3	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2008	0580, 0581	04

3			Accept all probability answers as fractions (non-reduced or reduced), decimals or percentages. -1 once for 2 sf answers or correct words. Condone numerical errors in simplifying or converting after correct answers seen. Ratio answers score zero throughout.
(a) (i)	$\frac{1}{3}, \frac{3}{8}, \frac{6}{8}, \frac{2}{8}$ o.e.	В3	−1 each error bod if no letters given
(ii)	$\frac{1}{3}, \frac{3}{8}, \frac{6}{8}, \frac{2}{8}$ o.e. $\frac{2}{3} \times \frac{5}{8}$ $\frac{5}{12}$ o.e. www2	M1 A1	$\frac{10}{24}$, etc., 0.416(6)
(iii)	their $\frac{5}{12} + \frac{1}{3} \times \frac{6}{8}$ $\frac{2}{3} \text{ o.e. cao} \qquad \text{www2}$	M1 A1	$\frac{16}{24}$, $\frac{8}{12}$, etc., 0.666(6)
(b) (i)	$\frac{3}{10} \times \frac{2}{9} \times \frac{1}{8}$ $\frac{1}{120} \text{ o.e.} \qquad \text{www2}$	M1 A1	$\frac{6}{720}$, etc., 0.00833(3)
(ii)	$\frac{119}{120}$ o.e.	B1ft	$\frac{714}{720}$, etc., 0.991(6) ft 1 – their (i) not for 7/10 Could start again and have a correct answer independently [10]

4 () ()	26 (26 0 26 4)	D1	
4 (a) (i)	36 (36.0–36.4)	B1	
(ii)	50 (50.0–50.4)	B 1	
(iii)	29 (28.6–29.4)	B 1	
(iv)	20	B2	If B0, SC1 for 19 or 21 or 180 seen
(b) (i)	p = 16, q = 4	B1,B1	If B0, SC1 if p and q add up to 20
(ii)	$\left(\frac{7220}{200}\right) = 36.1$ cso www4	B4	Answer 36 scores 4 marks after some correct working shown with no incorrect working seen M1 for using mid-values at least four correct from 5, 15, 25, 35, 45, 55, 65, 75 M1 (dep on correct mid values or mid-values ± 0.5) for $\sum fx$ (at least four correct products) M1 (dependent on 2^{nd} M1) for dividing sum by 200 or 180 + their p + their q
(c)	8.2 (8.19–8.20), 11.4 , 5 (5.00–5.01)	B4	B3 for 2 correct or B2 for 1 correct
			After B0, SC2 for fd's 2.7(3) o.e., 3.8 o.e, 1.6(6) o.e. or SC1 for 2 of fd's correct (15)
5 (a) (i)	$360 \div 8$ or $(8-2) \times 180$	M1	allow 6×180

Page 4	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2008	0580, 0581	04

	$180 - \text{their } (360 \div 8) \text{ o.e.} $ $\div 8$	M1	dependent
(ii)	45° used or use implied o.e.	E1	Accept sketch with values
(b) (i)	<i>l</i> 45	M1	For o.e. allow implicit expression
	$\frac{l}{12} = \cos 45$ o.e.		
	(PH =) 8.49 (8.485) www	A1	Accept $\sqrt{72}$, $2\sqrt{18}$, $3\sqrt{8}$, $6\sqrt{2}$
(ii)	$(PQ =) 2 \times \text{their } PH + 12 \text{ o.e.}$	M1	
	(PQ =) 29.(0) (28.96–29.00) ft www	2 A1 ft	ft their PH accept surd form
(iii)	their $PH \times \text{their } PH \div 2$ o.e.	M1	
	(Area $APH =$) 36 (35.95–36.1) ft www	2 A1 ft	ft their PH
(iv)	$(\text{their } PQ)^2 - 4 \times \text{their area of triangle o.e.}$	M2	If M0, M1 for a clear collection of areas
	(Area octagon =) 695 (694.0–697.1) cao		leading to the octagon possibly without
	www	3 A1	any calculation shown
(c) (i)	0.5 of their PQ o.e.	M1	e.g. $6 + PH$, $6 \tan 67.5^{\circ}$
	14.5 (14.47–14.53) cao www	2 A1	accept surd form
(ii)	$\pi \times (their r)^2$	M1	(660.5)
	their circle area ×100	M1	Dependent on first M1 and circle smaller
	their octagon area	1411	than the octagon
	94.8 (94.35 to 95.60) cao www	3 A1	[17]

6 (a) (i)	$\begin{pmatrix} 2 \\ 1 \end{pmatrix}$	B1	Allow (2 1), condone omission of brackets
(ii)	$\begin{pmatrix} 2 \\ 1 \end{pmatrix}$ ft	B1ft	Allow (2 1), condone omission of brackets ft their (i) if a vector
(b)	Translation $\begin{pmatrix} 0 \\ -4 \end{pmatrix}$ o.e.	B1, B1	Allow (0 –4), condone omission of brackets, allow in words Any extra transformation spoils both marks
(c)	y > 0 o.e. x < 2 o.e. $y > \frac{1}{2}x$ o.e. y < 2x + 4 o.e.	B1 B1 B1	For all four, condone strict inequalities and only penalise first incorrect sign, which may be = or an inequality sign If B0, B1 for $2x$ or for 4 if other
			co-efficient is not zero $y < \frac{1}{2}x + 4 \text{gets zero} $ [9]

7 (a) (i)	cyclic		B1	Condone concyclic
(ii)	Any one of 40 , 45 , 50		B1	Angle $BCT = 40^{\circ}$ is inconsistent with ST
	Any one of 20 , 25 , 30		B1	parallel to OB. So different values of
	Any one of 105 , 110 , 115		B1	angles x , y , z , OCT and AOC can be
				arrived at, depending on route taken.
(iii)	Any one of 80 , 85 , 90		B 1	
(iv)	Any one of 210 , 215 , 220 , 225 , 230		B1	
(b) (i)	Similar (or enlargement)		B1	
(ii)	$\left(\frac{7}{10}\right)^2$ or $\left(\frac{10}{7}\right)^2$ o.e. seen		M1	(0.49), (2.04)
		ww2	A1	It is possible to do (iii) then (ii) and full marks can still be scored
(iii)	1 10 1 1 20		M1	
	$\frac{1}{2} \times 10 \times height = 20$		A1	
	- -	ww2		[11]

Page 5	Mark Scheme	Syllabus	Paper
	IGCSE – May/June 2008	0580, 0581	04

8 (a)		M1	M1 for method of compound interest used
、 /	108 (.16) (allow 108.2(0)) www2	A1	•
(b)	148 (.02) 324 (.3)	B1 B1	
(c)	Correct axes full domains	S1	Condone absence of labels
	5 correct pts 100, 148 ft, 219, 324ft, 480	P3ft	P2ft for 4 correct, P1ft for 3 correct
	_		Points must be in correct square vertically,
			including on line
	Smooth exponential curve, correct shape	C 1	Scale error – remove that part and try to
	through 5 points		mark the rest
(d) (i)	265 – 270	B1ft	If out of range, then ft their graph at 25
			years
(ii)	17 or 18 cao	B1	
(e) (i)	$(100) \times 7 \times 20$		
	(100) o.e.	M1	
	$100 + 7 \times 20$ or better	E1	No errors
(ii)	380	B1	
(iii)	Correct straight ruled line for x – range 0 to	L2	P1ft for 2 of (0,100), (20,240) (40,380)ft
	35		correctly plotted
(f)	27 – 29 cao	B1	[17]

9 (a) (i)	p + r	B1	Answers in bracketed column form penalise only once throughout
(ii)	$-\mathbf{p}+\mathbf{r}$	B1	
(iii)	$-\mathbf{p} + \frac{2}{3}\mathbf{r}$	B1	
(iv)	$\mathbf{p} + \frac{1}{2}\mathbf{r}$	B1	
(b) (i)	$\frac{3}{2} \times (-\mathbf{p} + \frac{2}{3}\mathbf{r}) \text{ or } -\frac{3}{2}\mathbf{p} + \mathbf{r} \text{ isw after}$ correct answer seen	B1 ft	ft only $\frac{3}{2}$ × their (a)(iii)
(ii)	$\overrightarrow{QP} + \overrightarrow{PS}$ o.e.	M1	o.e. is any correct route of at least 2 vectors
	$-\frac{3}{2}\mathbf{p}$ www 2	A1 ft	ft their (b)(i) – r
(c)	lie on a straight line	B1	dependent on their (b)(ii) being a multiple of p [8]

10(a) (i)	4	B1	
(ii)	24	B1	
(b) (i)	x + 12, x + 14 o.e.	B1,B1	Any order ignore ref to g and i
(ii)	(x+14-x) and $(x+12-(x+2))$		x + 12 and $x + 14$ must be seen to be used
	14 – 10 or 14 – 12 + 2 or 4	E 1	No errors seen
(iii)	(x+2)(x+12) - x(x+14)	B1	Subtraction can be implied later
	24	E1	Dep on B1 and no errors anywhere for the E mark
(c) (i)	4	B1	
(ii)	20	B1	
(d) (i)	4	B1	
(ii)	x + 2n o.e., $x + 2 + 2n$ o.e.	B1,B1	
(iii)	4 <i>n</i>	B1	Allow $4 \times n$, $n \times 4$, $n4$ [13]